

INSTRUCTION:

- a. Answer the following questions on the answer paper provided by the exam committee
- b. During work you can open one note in a note sheet on A4 paper.
- c. Can use a calculator but may not use a cell phone during the TEST

1. An electron with mass $m = 9.1 \times 10^{-31} \text{ kg}$ moves after the system is heated to 500 K . Determine the wavelength de Broglie electrons (Boltzmann's constant $k = 1.38 \times 10^{-23} \text{ J/K}$ and Planck's constant $h = 6.63 \times 10^{-34} \text{ Js}$)

Hint: The kinetic energy of an electron is the same as the thermal energy of an electron and consider the electron as a single particle.

2. The wave deviation function is expressed as:

$$\Psi(x) = \begin{cases} \sqrt{\frac{2}{L}} \sin \frac{\pi x}{L} & 0 < x < L \\ 0 & \text{etc} \end{cases}$$

- a. Calculate the positional uncertainty as $\Delta x = \{\langle x^2 \rangle - \langle x \rangle^2\}^{1/2}$
- b. Calculate the momentum uncertainty as: $\Delta p = \{\langle p^2 \rangle - \langle p \rangle^2\}^{1/2}$
- c. Prove that for the wave function above we get the equation Heisenberg uncertainty

$$\Delta x \Delta p_x \geq \frac{h}{2}$$

Hint: The average function can be calculated from:

$$\langle x \rangle = \int_{-\infty}^{\infty} x |\Psi(x)|^2 dx \quad \text{dan} \quad \langle p_x \rangle = \int_{-\infty}^{\infty} |\Psi^*(x)| \frac{h}{i} \frac{\partial}{\partial x} \Psi(x) dx$$

3. Show that there is no negative energy solution for the yang particle trapped in a well of potential energy

$$V(x) = \begin{cases} 0 & 0 < x < L \\ \infty & \text{etc} \end{cases}$$